Decentralized Systems Engineering

CS-438 – Fall 2025

DEDIS

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EPFL

Credits: D. Ongaro, J. Ousterhout, L. Alvisi, A. Ghodsi, D. Mazières, L.Q. Torres, et al.

So far...

- Decentralized communication
- Unstructured & structured search
- Data storage

Let’s pick up where we left off ...

Conflict-Free Replicated Data Types (CRDTs)

Various types:

- Values
- Counters
- Sets
- Lists
- Log-based
- Text

Two main categories:

- Operation-based – commutative replicated data types (CmRDTs)
- State-based – convergent replicate data types (CvRDTs)

→ Theoretically equivalent

State-based CRDT – Formalism

Let U be the set of update operations, and V the set of values.

A state-based CRDT is a 5-tuple (S, s^0, q, u, m), where:

- S is the set of states;
- $s^0 \in S$ is the initial state;

- $q : S \rightarrow V$ is the **query** function
- $u : S \times U \rightarrow S$ is the **update** function
- $m : S \times S \rightarrow S$ is the **merge** function

G-Counter CRDT

Specifications:

- Grow-only counter,
  replicated across N machines
- Add(x)
  updates our local counter
- Query() returns the value
- Merge(other_state)
  merge's other's state

```
class GCounter(object):
  def __init__(self, i, n):
    self.i = i # server id
    self.n = n # number of servers
    self.xs = [0] * n

  def add(self, x):
    assert x >= 0
    self.xs[self.i] += x

  def query(self):
    return sum(self.xs)

  def merge(self, other):
    zipped = zip(self.xs, other.xs)
    self.xs = [max(x, y) for (x, y) in zipped]
```

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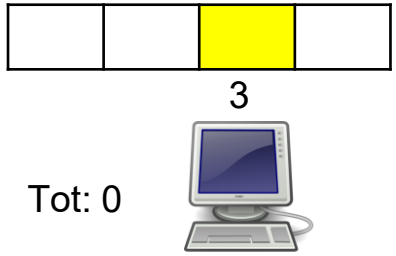

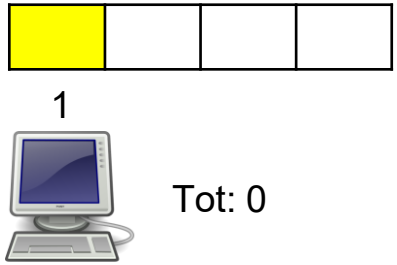

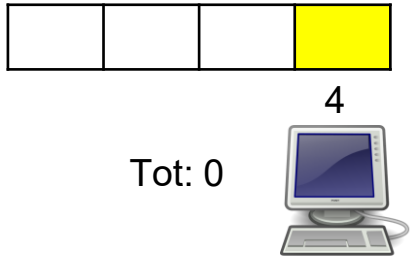

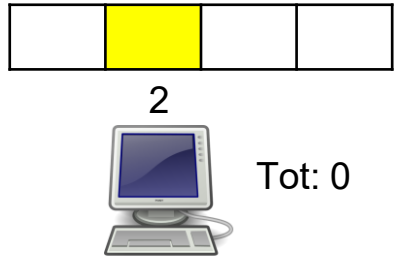

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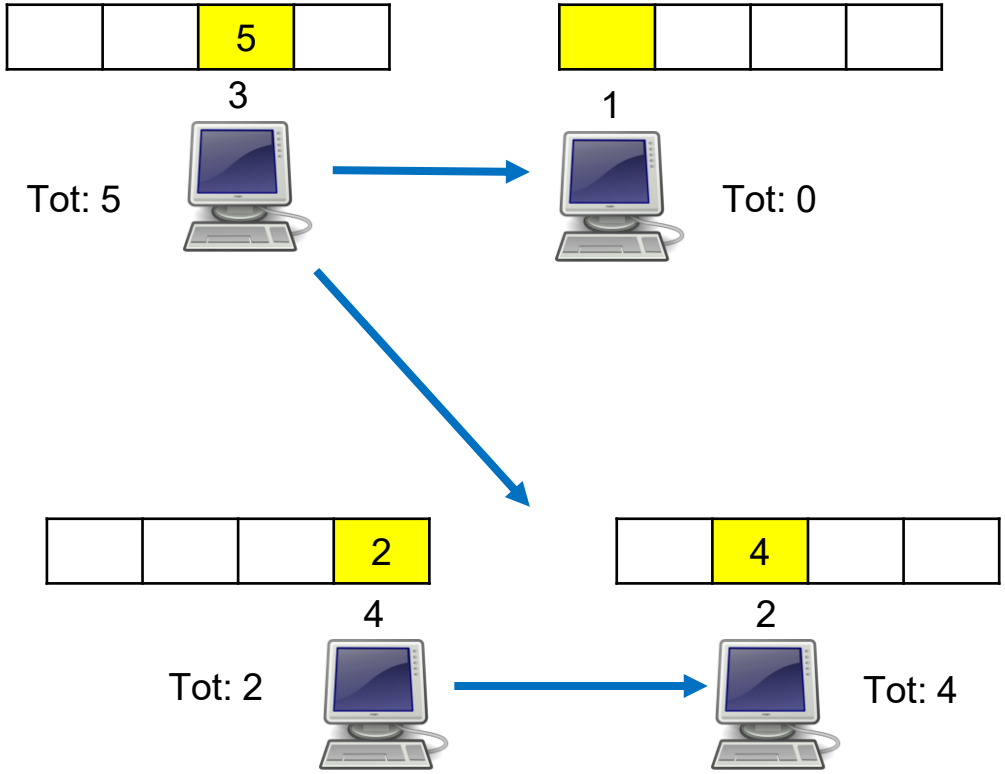

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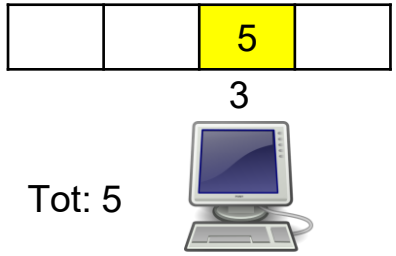

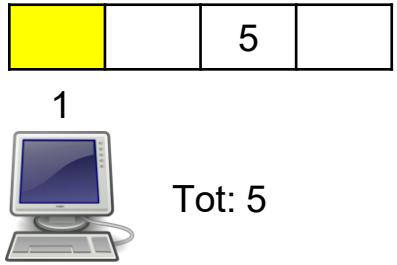

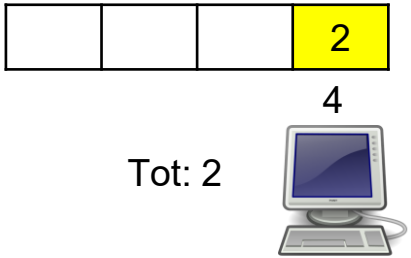

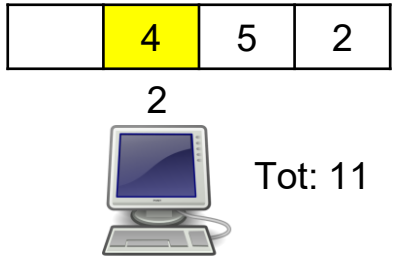

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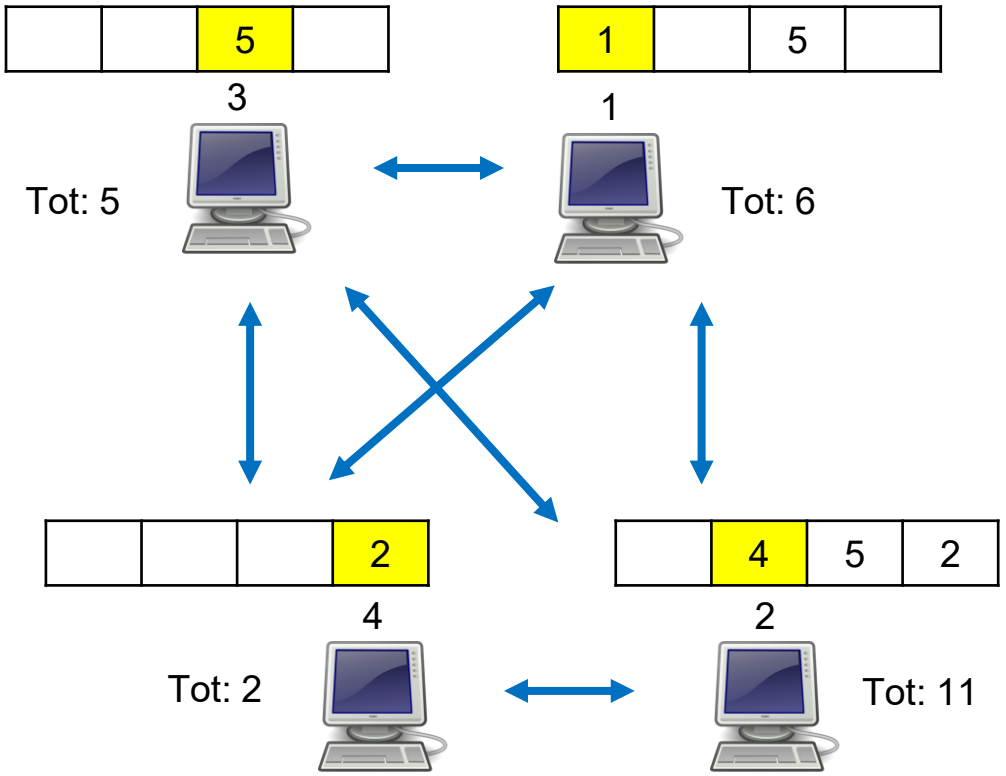

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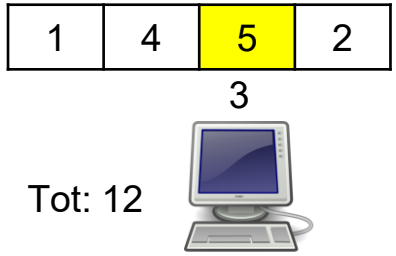
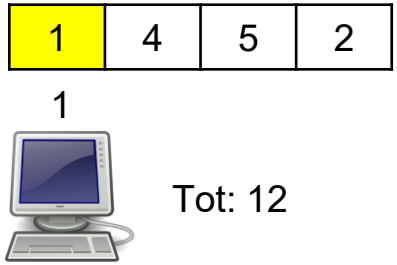
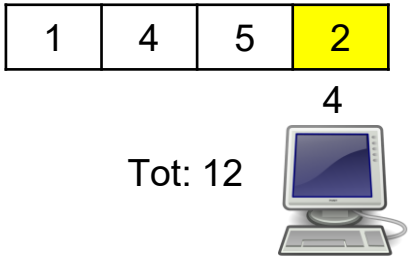
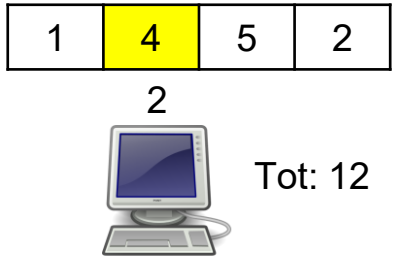




History, as seen locally:

Node 1: 0 → 5 → 6 → 12
Node 2: 0 → 4 → 11 → 12
Node 3: 0 → 5 → 12
Node 4: 0 → 2 → 12





… eventually consistent !

Local-First Software – simpler backends

Consistency ?

- What if we wanted a shared history of the “state” ?

  Google Docs approach:

  → centralize

  → use time stamps

  → does not ensure consistency

- How could we stay distributed (or even decentralized) and be consistent ?
- How could we build the *same, incremental* history of the state ?

  Today’s lecture: Replication and consensus !

Replication and Consensus

Paxos

(Homework 3)

Consistent Data Replication

You know of:

- Redundant Array of Independent Disks (RAID)
- Centralized, distributed databases (Master/slave replication)

Our goal, decentralization:

- No privileged “master”
- Replicated & **consistent** data

→ Hard problem, requires **consensus**

Consensus

- Consensus is agreeing on **one** result
- Once a **majority** agrees on a proposal, that is consensus
- The consensus is **eventually** known by everyone
- Involved parties want to agree on **any** result, not just their own

  ... in the presence of failures

- Types

  Permissioned (today) – known nodes

  Permissionless (week 9 & 10) – anyone

Single-value Consensus (formally)

We want all nodes (“processes”) to agree on a single value

- **Agreement / Safety**

every *correct* process must agree on the same value

- **Termination / Liveness**

eventually, every *correct* process decides some value

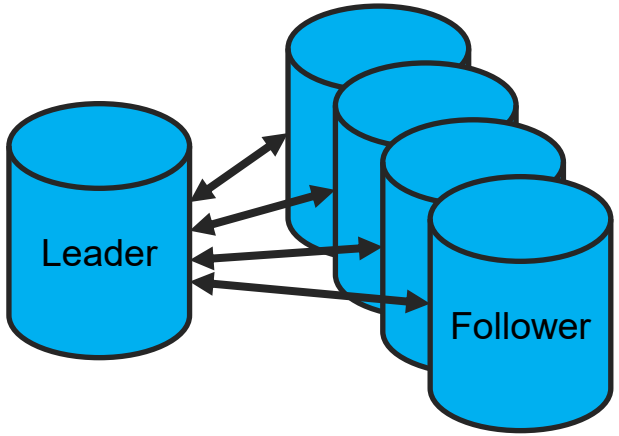
- **Integrity / Validity** (weak / strong / ...)

If all *correct* processes proposed value X, then *correct* processes must decide X
If a *correct* process decides X, then X must have been proposed by correct process

- f processes can fail → failure model?

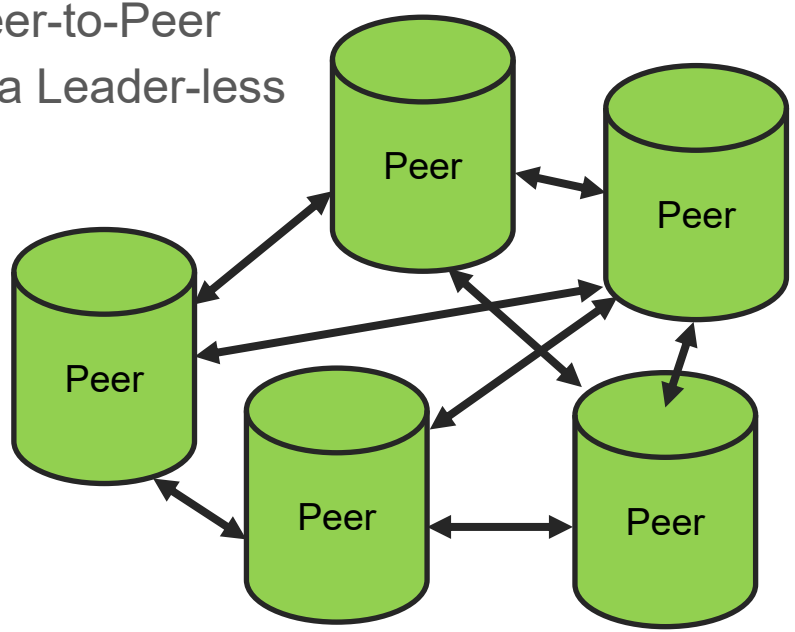
Types of (permissioned) consensus

- Leader-based



- Electing/rejecting leader is tricky, and requires consensus
- “Following” is easy & efficient

- Peer-to-Peer
  aka Leader-less



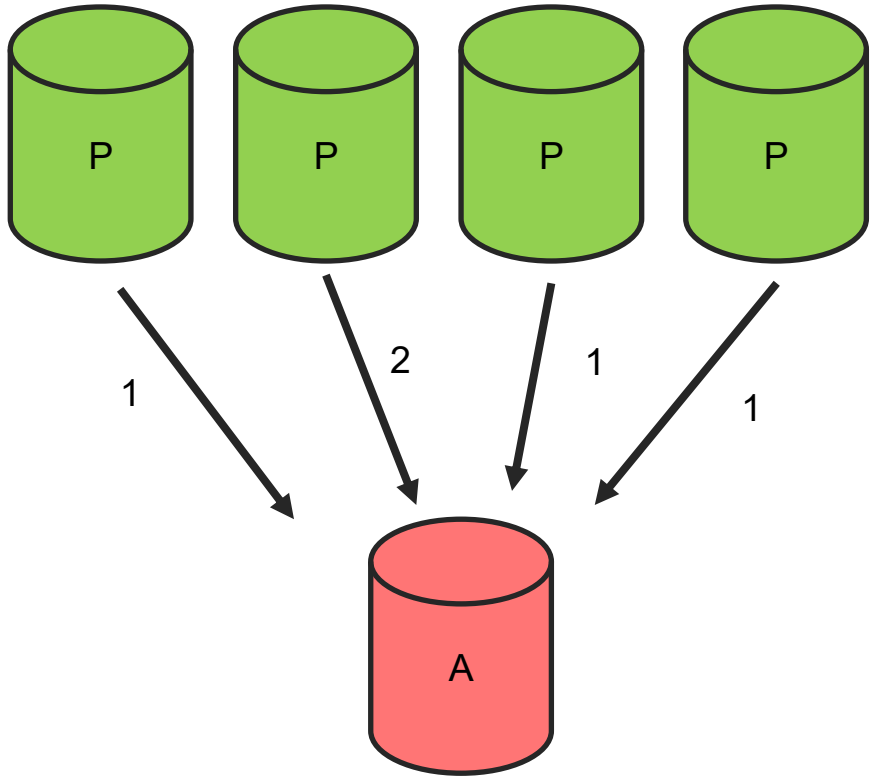
- Consensus is needed continuously
- No “extra” work when node fails

Building a consensus...

Easy (and wrong) !

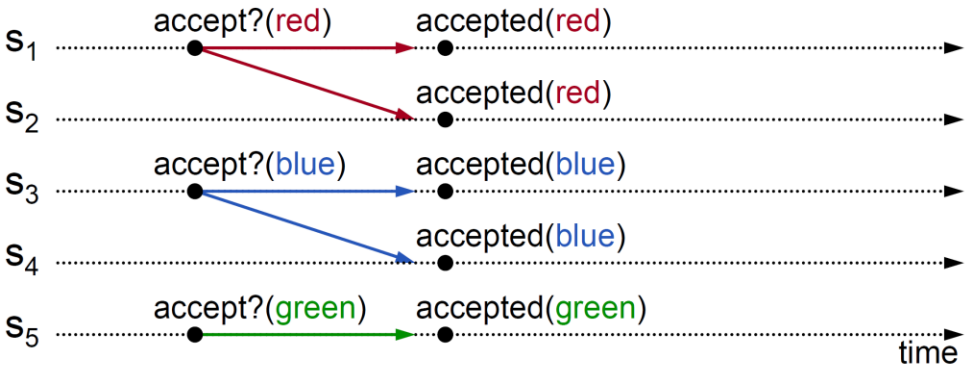
- All “proposers” node vote
- One acceptor choses the value

What if the acceptor crashes
... before choosing ?
... after choosing ?



Building a better consensus...

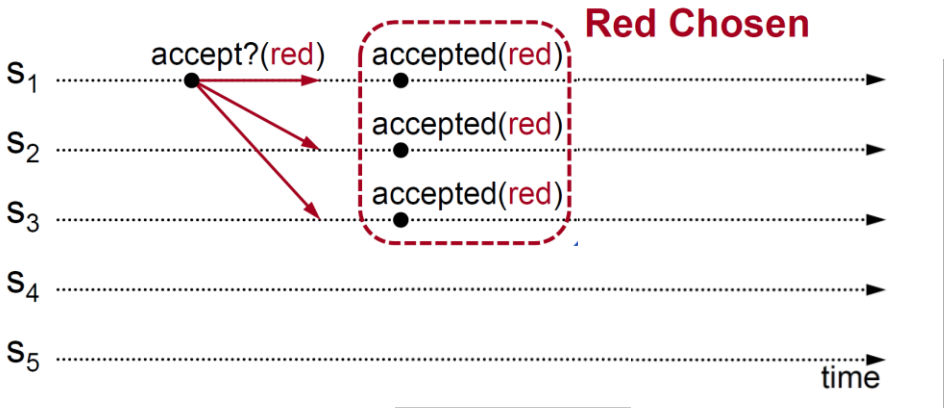
- All “proposers” node vote
- Multiple “acceptors” node
- Value is chosen if accepted by majority



Easy (and still wrong) : split votes !

Building a better consensus ?

- Same as before
- Now, “acceptors” nodes accept **every** value they receive
- Value is chosen if accepted by majority



- We need a **two-phase** protocol !

Paxos

- A family of distributed algorithms for consensus

Three roles:

- Proposers: put forth values to be chosen
- Acceptors: respond to proposers, reach consensus
- Learners: learn the agreed upon value

- Nodes can take any (or even all) roles
- Nodes must know how many acceptors make up a majority
- Nodes must be persistent: they can’t walk back on

Paxos phases : intuition

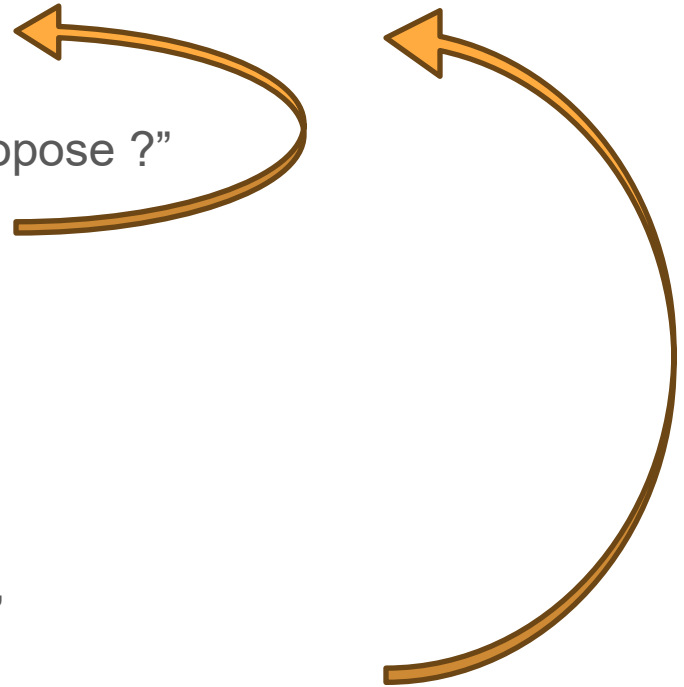
- Prepare phase

  Proposer: “Will you consider a value I propose ?”
  Each acceptor: “Okay” / “Nope...”

If a majority is obtained:

- Accept phase

  Proposer: “Here’s my proposed value: X”
  Acceptors: “Okay for X !” / “Nope!”



The Paxos Algorithm

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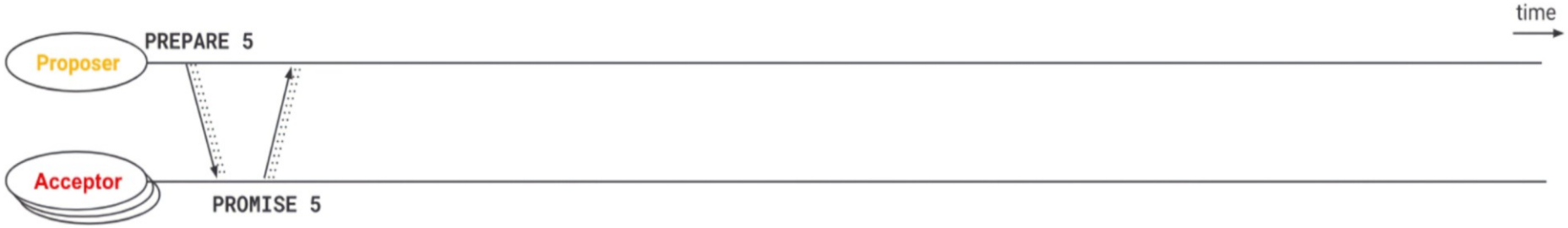

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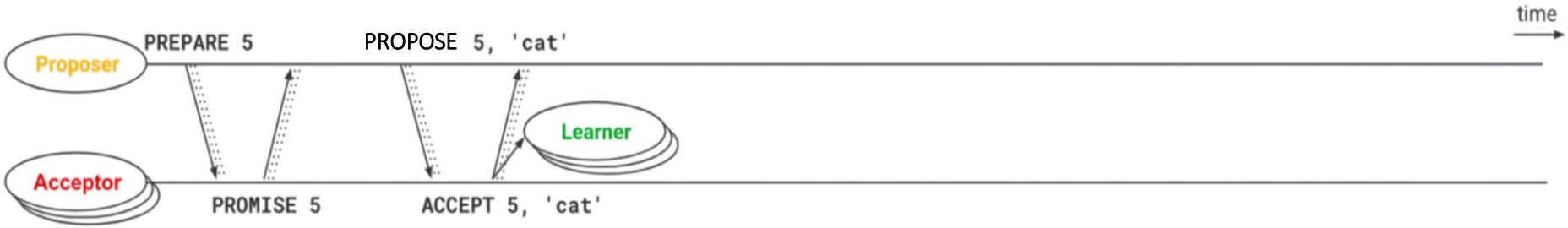

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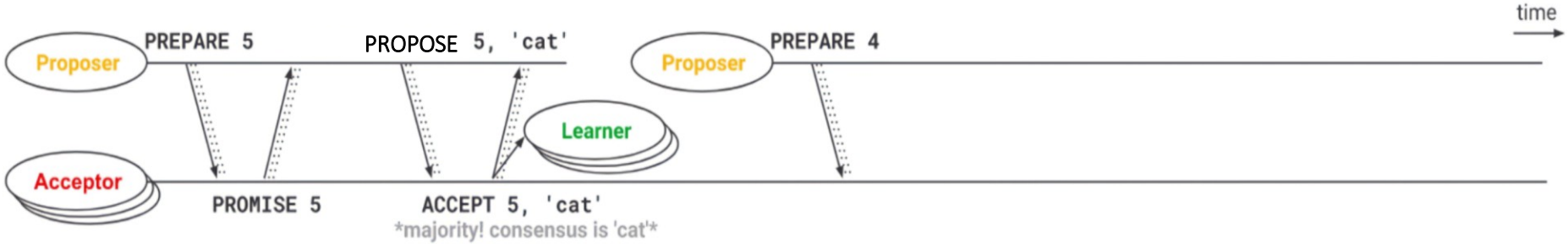

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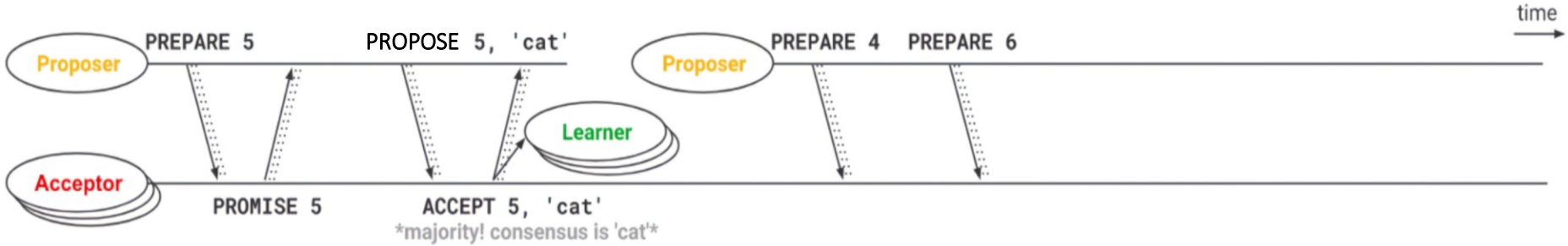

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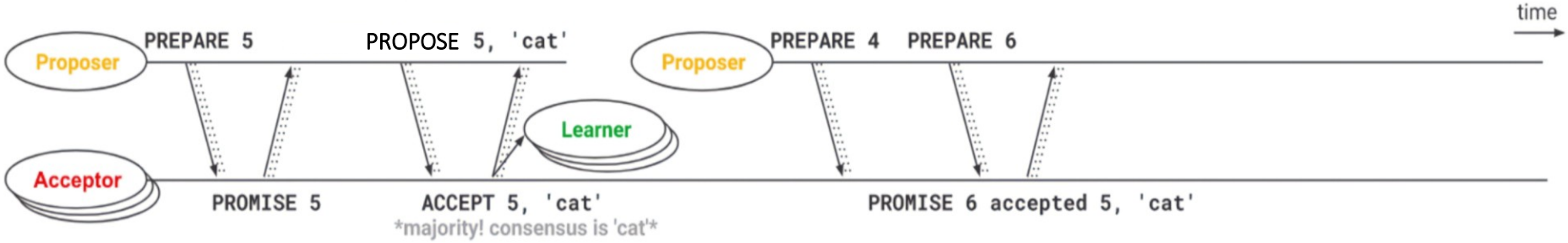

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Has it got any already accepted value from promises?
Yes - > It picks the value with the highest **IDa** that it got.
No -> It picks any value it wants.

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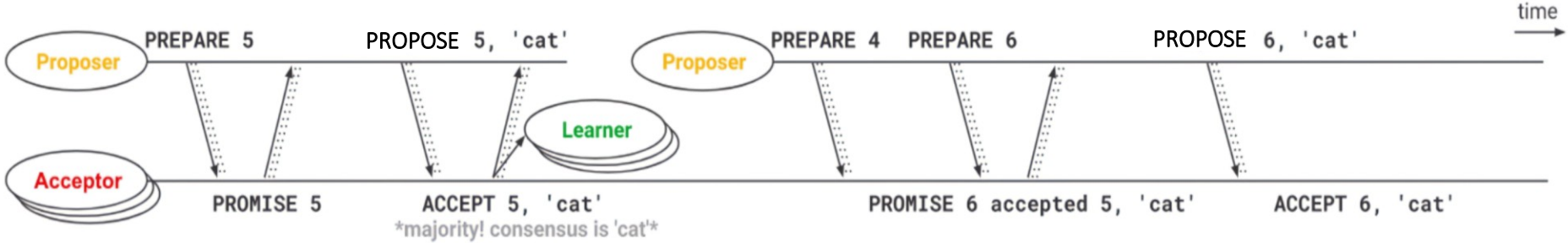
The Paxos Algorithm



⇨ **Proposer** wants to propose a certain value:
It sends **PREPARE** **IDp** to a majority (or all) of **Acceptors**.
IDp must be unique, e.g. slotted timestamp in nanoseconds.
e.g. **Proposer** 1 chooses IDs 1, 3, 5...
Proposer 2 chooses IDs 2, 4, 6..., etc.
Timeout? retry with a new (higher) IDp.

⇨ **Acceptor** receives a **PREPARE** message for IDp:
Did it promise to ignore requests with this IDp?
Yes -> then ignore
No -> Will promise to ignore any request lower than IDp.
Has it ever accepted anything? (assume accepted ID=**IDa**)
Yes ->Reply with **PROMISE** **IDp** **accepted** **IDa**, **value**.
No -> Reply with **PROMISE** **IDp**.

1 **If a majority of acceptors promise, no ID<IDp can make it through.**

⇨ **Proposer** gets majority of **PROMISE** messages for a specific IDp:
It sends PROPOSE **IDp**, **VALUE** to a majority (or all) of **Acceptors**.
Has it got any already accepted value from promises?
Yes - > It picks the value with the highest **IDa** that it got.
No -> It picks any value it wants.

⇨ **Acceptor** receives an PROPOSE message for IDp, value:
Did it promise to ignore requests with this IDp?
Yes -> then ignore
No -> Reply with **ACCEPT** **IDp**, **value**. Also send it to all **Learners**.

2 **If a majority of acceptors accept IDp, value, consensus is reached. Consensus is and will always be on value (not necessarily IDp).**

⇨ **Proposer** or **Learner** get **ACCEPT** messages for IDp, value:

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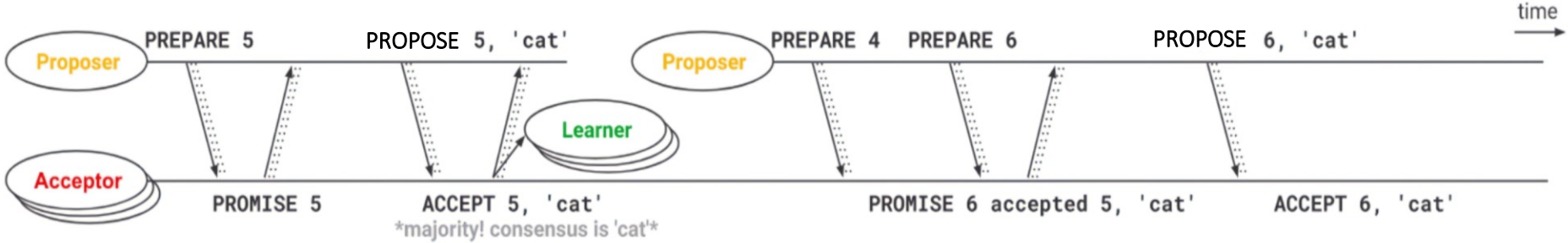
The Paxos Algorithm



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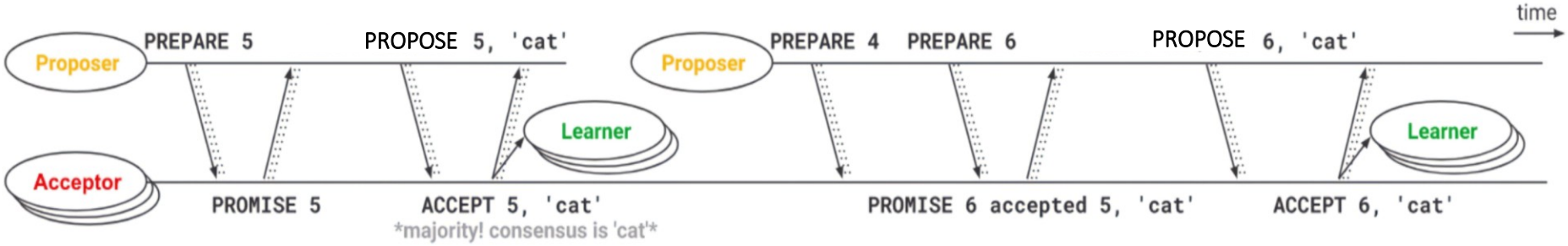

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Surviving node failures

How many nodes do you need ?

Paxos Challenges

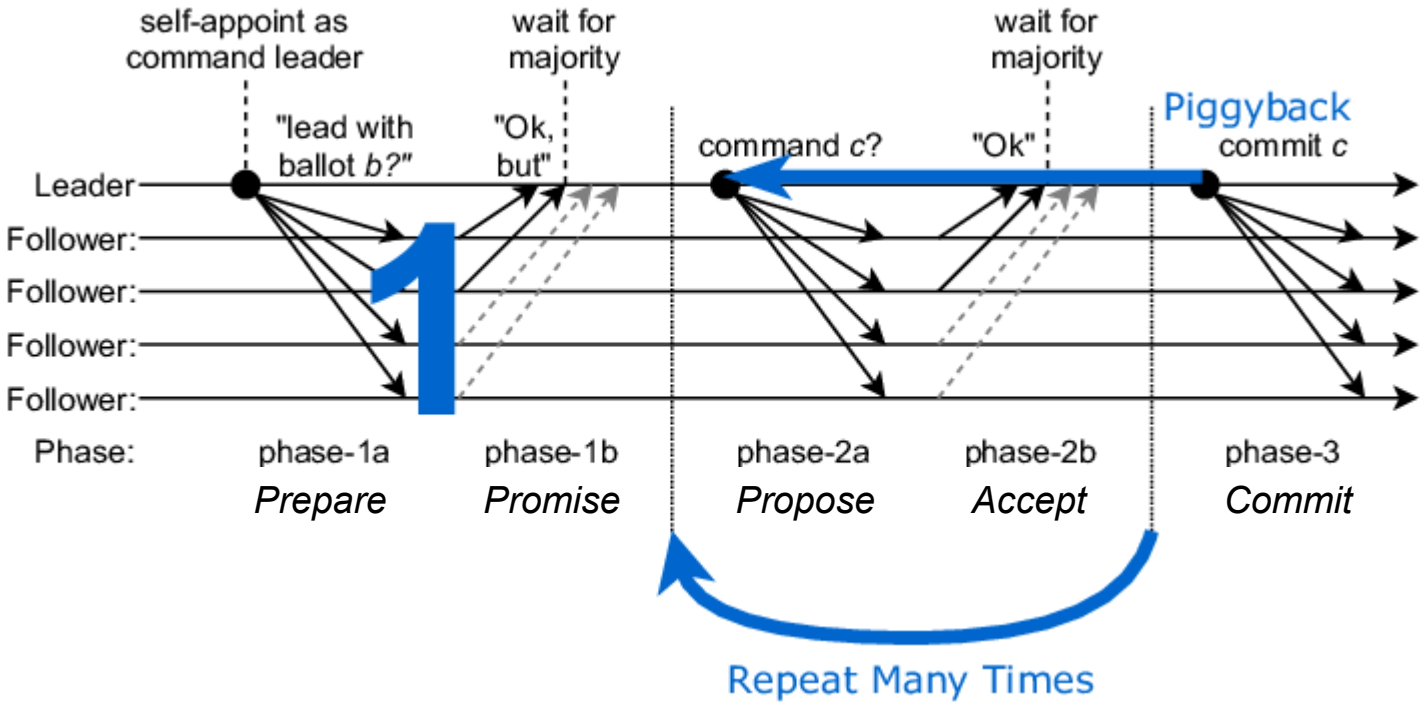
- Contention

- Non crash-stop behaviour
  - Asynchrony
  - Byzantine faults

- (In)efficiency of simple Paxos
  - Introducing a leader
  - Protocol “Quick wins”

- Choosing multiple, subsequent values (e.g. Multi-Paxos)

Multi-Paxos: Leader-based optimization



Source: A. Charapko, PigPaxos

Paxos: recap

Key properties:

- Safety: all nodes agree on a (single) decision
- Liveness: eventually something is decided

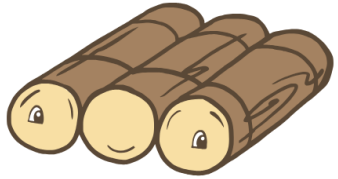
Assumptions:

- Crash-stop model
- Partially synchronous
- # acceptors = 2f + 1

Protocol (choose 1 value):

- Phase 1: Prepare/Promise
- Phase 2: Propose/Accept

The Raft Consensus Algorithm



- Designed to be easy to understand
- Functionally equivalent to Paxos
- Easier to implement (claim)
- Widely used in the industry
  MongoDB, CockroachDB
  Etcd, Neo4j, RabbitMQ
  ...